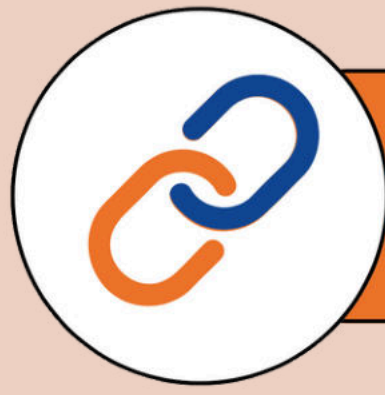


RAS
Prelims



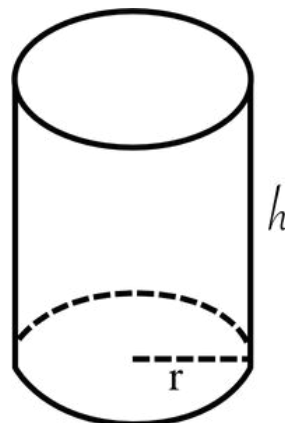
Connect
Civils RAS

RAS
Prelims

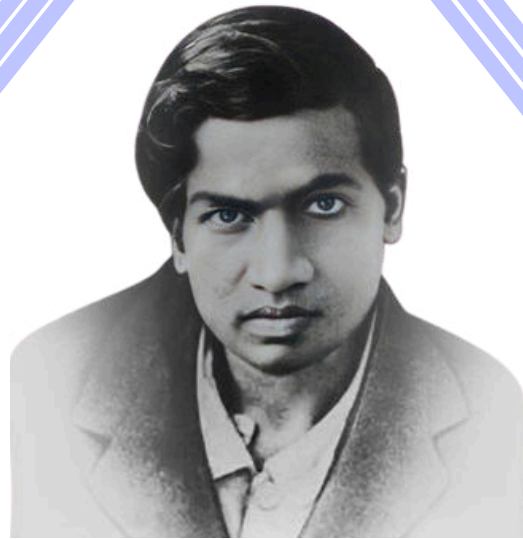
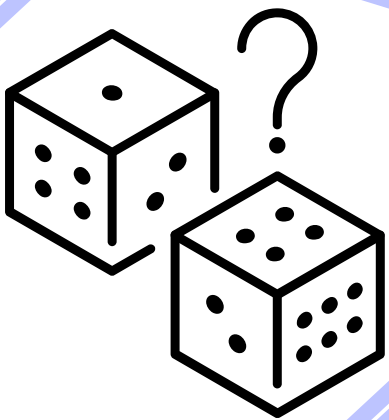
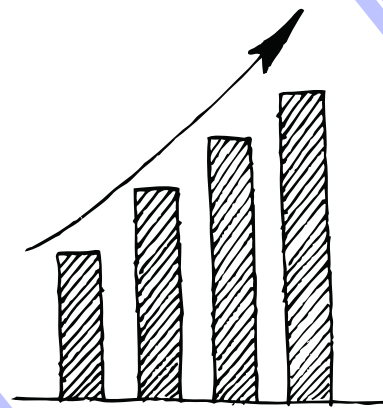
Complete coverage of standard books, RBSE, NCERT..

Basic Numeracy (Maths) Question Bank

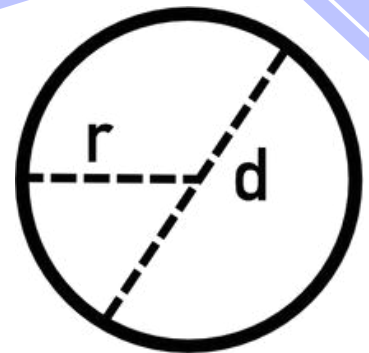
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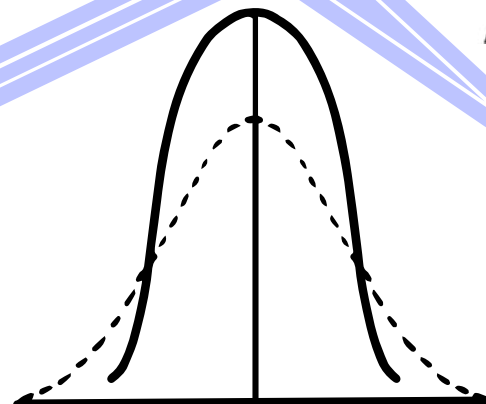
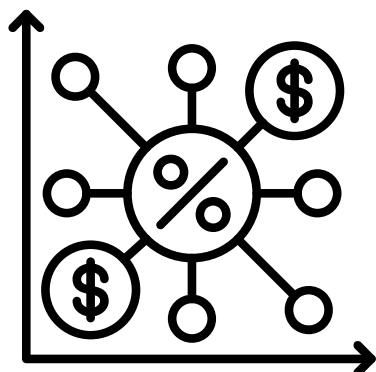
$$V = \pi r^2 h$$



Srinivasa Ramanujan



$$A = \pi r^2$$



Mean Median
Mode

Download App for all subject notes (IAS/RAS)



9352179495



Connect Civils RAS



Youtube Lecture



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Ratio & proportion

1. A and B invest in a business in the ratio 3 : 2. If 5% of the total profit goes to Charity and A's share is Rs. 8,550, then total profit is -
- (A) Rs. 15,760
 (B) Rs. 15,000
 (C) Rs. 14,250
 (D) Rs. 15,735
 (E) Question not attempted

Ans (B)**Explanation:**

Given:

Investment ratio of A and B = 3 : 2

5% of the total profit goes to Charity

A's share = Rs. 8,550

Formula used:

Total profit = (A's share / A's ratio) × Total ratio

Calculation:

Let the total profit be P.

Charity = 5% of P

Profit after charity = 95% of P

A's share = (A's ratio/total ratio)*total profit = $(3 / (3 + 2)) \times 95\%$ of P

$$\Rightarrow 8,550 = (3 / 5) \times 0.95P$$

$$\Rightarrow 8,550 = 0.57P$$

$$\Rightarrow P = 8,550 / 0.57$$

$$\Rightarrow P = 15,000$$

∴ The total profit is Rs. 15,000

2. A sum of money is to be distributed among A, B, C, D in the proportion of 5 : 2 : 4 : 3. If C gets Rs. 1000 more than D, what is B's share?

- (A) Rs. 500
 (B) Rs. 1500
 (C) Rs. 2000
 (D) Rs. 2000
 (E) Question not attempted

Ans (C)**Explanation:**

Given:

money is to be distributed among A, B, C, D in the proportion of 5 : 2 : 4 : 3

C gets Rs. 1000 more than D

Calculation:

Let the shares of A, B, C and D be Rs. 5x, Rs. 2x, Rs. 4x and Rs. 3x respectively.

C's share - D's share = 1000

Then, $4x - 3x = 1000$ $x = 1000$.

B's share = Rs. 2x = Rs. (2 x 1000) = Rs. 2000.

3. A, B and C enter into a partnership in the ratio $\frac{7}{2} : \frac{4}{3} : \frac{6}{5}$. After 4 months, A increases his share 50%. If the total profit at the end of one year be Rs. 21,600, then B's share in the profit is:

- (A) Rs. 2100
 (B) Rs. 2400
 (C) Rs. 3600
 (D) Rs. 4000
 (E) Question not attempted

Ans (D)**Explanation:**Initially ratio of A B and C is $\frac{7}{2} : \frac{4}{3} : \frac{6}{5}$.

after simplifying this ratio is 105x:40x:36x

after four month A increases his share by 50%

Ratio of their profit is

$$(105x * 4) + (150/100 * 105x * 8) : (40x * 12) : (36x * 12)$$

$$105*16:40*12:36*12$$

35:10:9

B's share = (B's ratio/total ratio)*total profit

B's share = $10/54 * 21600 = 4000$

**Percentage**

1. A, B and C jointly thought of engaging themselves in a business venture. It was agreed that A would invest Rs. 6500 for 6 months, B, Rs. 8400 for 5 months and C, Rs. 10,000 for 3 months. A wants to be the working member for which, he was to receive 5% of the profits. The profit earned was Rs. 7400. Calculate the share of B in the profit.

- (A) Rs. 1900
 (B) Rs. 2660
 (C) Rs. 2800
 (D) Rs. 2840
 (E) Question not attempted

Ans (B)**Explanation:**

For managing, A received = 5% of Rs. 7400 = Rs. 370.

Balance = Rs. (7400 - 370) = Rs. 7030.

Ratio of their investments = (6500 x 6) : (8400 x 5) : (10000 x 3)

Ratio of their investments = 39000 : 42000 : 30000

Ratio of their investments = 13 : 14 : 10

B's share = (B's ratio/total ratio)*total profit

B's share = 7030*14/37=2660 Rs

2. A, B and C started a business each investing Rs.10000. After 4 month A withdraws Rs.3000, B withdraws Rs.4000, C invest Rs.3000 more At the end of the years, a total profit was Rs.32800. Find the share of C.

- A) Rs. 11400
 B) Rs. 14000
 C) Rs. 16000
 D) Rs. 14400
 E) Question not attempted

Ans (D)**Explanation:**

Ratio of capital of A, B and C.

= (10,000 x 4 + 7000 x 8) : (10,000 x 4 + 6000 x 8) : (10,000 x 4 + 13000 x 8)

= 96000 : 88000 : 144000

So, Ratio becomes 12 : 11 : 18

Distributing the final profit of Rs. 32800 in the given ratio,

The share of C = (C's ratio/total ratio)*total profit

The share of C = 18/41*32800 = 14400

3. Person A started a business by investing Rs. 65,000. After a few months, B joined him by investing Rs. 50,000. Three months after the joining of B, C joined the two with an investment of Rs. 55,000. At the end of the year, A got 50% of profit as his share. For how many months did A alone finance the business?

- (A) 4
 (B) 2
 (C) 5
 (D) 3
 (E) Question not attempted

Ans (D)**Explanation:**

given:

Person A started a business by investing Rs. 65,000.

After a few months, B joined him by investing Rs.

50,000.

Three months after the joining of B, C joined the two with an investment of Rs. 55,000.

A got 50% of profit as his share.

Formula used:

Profit ratio = Investment1 x Time1 : Investment2 x Time2 : Investmentn x Timen

Calculation:

Let B invest the amount after x months

A invest for 12 month

B invest for (12 - x) months

Three months after the joining of B, C joined the two with an investment of Rs. 55,000.

C invest for (12 - x - 3) ⇒ (9 - x)

Profit share = A : B : C

Profit share = 65,000 x 12 : 50,000 x (12 - x) : 55,000 x (9 - x)

⇒ 156 : 10(12 - x) : 11(9 - x)

A got 50% of profit as his share

⇒ 156/(156 + 120 - 10x + 99 - 11x) = 1/2

⇒ 312 = 375 - 21x

⇒ 21x = 63

⇒ x = 3 month

or

156 = 10(12 - x) : 11(9 - x)

156 = 219 - 21x

21x = 63

x = 3

∴ A alone finance the business for 3 month.

**Simple & Compound Interest**

1. A sum of money was lent at simple interest at 11% per annum for $7\frac{1}{2}$ years and $9\frac{1}{2}$ years, respectively. If the interest difference for two periods was Rs. 5500, find the sum.

- (A) 40000
 (B) 50000
 (C) 60000
 (D) 45000
 (E) Question not attempted

Answer:- (B)**Explanation:-**

Let P be the sum of money lent.

Given,

Rate of interest per annum (R) = 11%

Interest earned in $9\frac{1}{2}$ years – Interest earned in $7\frac{1}{2}$ years = Rs. 5500

Using simple interest formula, we have;

$$P \times (9\frac{1}{2}) \times 11 \times (1/100) - P \times (7\frac{1}{2}) \times 11 \times (1/100) = \text{Rs. } 5500$$

$$(P/200) [99 - 77] = \text{Rs. } 5500$$

$$22P/200 = \text{Rs. } 5500$$

$$P = (\text{Rs. } 5500 \times 200)/22 \\ = \text{Rs. } 50000$$

Therefore, the required sum is Rs. 50000

2. A bank offers 5% compound interest calculated on half-yearly basis. A customer deposits Rs.1600 each on 1st January and 1st July of a year. At the end of the year, the amount he would have gained by way of interest is?

- (A) Rs.121
 (B) Rs.120
 (C) Rs.123
 (D) Rs.122
 (E) Question not attempted

Answer:- (A)**Explanation:-**

Given : rate of interest 5%

principal = 1600

first case: time=1 year

for half yearly compound interest

$$\text{time}=2*t=2*1=2$$

$$\text{rate of interest}=R/2=5/2$$

$$A=P(1 + R/100)^n$$

$$A=1600[1+5/200]^2$$

$$A=1600*41/20*41/40=1681$$

$$CI=A-P = 1681-1600=81$$

second case : time = $\frac{1}{2}$

for half yearly compound interest

$$\text{time}=2*t=2*\frac{1}{2}=1$$

$$\text{rate of interest}=R/2=5/2$$

$$A=P(1 + R/100)^n$$

$$A=1680[1+5/200]$$

$$A=1680*41/40$$

$$A=1640$$

$$CI=A-P = 1640-1600=40$$

from first and second case

$$\text{total gain}=81+40=121$$

3. Mihir's capital is $\frac{5}{4}$ times more than Tulsi's capital. Tulsi invested her capital at 50 % per annum for 3 years (compounded annually). At what rate % p.a. simple interest should Mihir invest his capital so that after 3 years, they both have the same amount of capital?
- (A) $20\frac{1}{3}$ %
 (B) 10 %
 (C) $50\frac{1}{3}$ %
 (D) 1.728 %
 (E) None of these

Answer:- (C)**Explanation:-**

Given

Mihir's capital is $\frac{5}{4}$ times more than Tulsi's capital.

suppose Tulsi's capital=4x

$$\text{Mihir's capital}=\frac{5}{4}*4x+4x=9x$$

In Tulsi's case

$$A=P(1 + R/100)^n$$

$$A=4x[1+50/100]^3=4x*3/2*3/2*3/2 \text{ -----1}$$

In Mihir's case

$$A=P+SI=9x+9x*R*3 \text{ -----2}$$

from 1 and 2 cases

$$4x*27/8=9x*[1+3R]$$

$$3/2=1+3R$$

$$3R=1/2$$

$$R=1/6$$

$$R\%=100/6=50/3$$

4. A sum of Rs. 800 amounts to Rs. 920 in 3 years at simple interest. If the interest rate increases by 3%, what will be the amount?
- (A) 828

**Perimeter & Area Of Plane Figures**

1. A rectangular park of length 30 m and breadth 25 m has a path of uniform width 5 m around its perimeter. Find the cost of tiling the whole path if the cost of tiling per 10 m² is ₹ 1500.
- (A) 97500
 (B) 97000
 (C) 96500
 (D) 98500
 (E) Question not attempted

Ans (A)**Explanation:**

Length of the park = 30 m

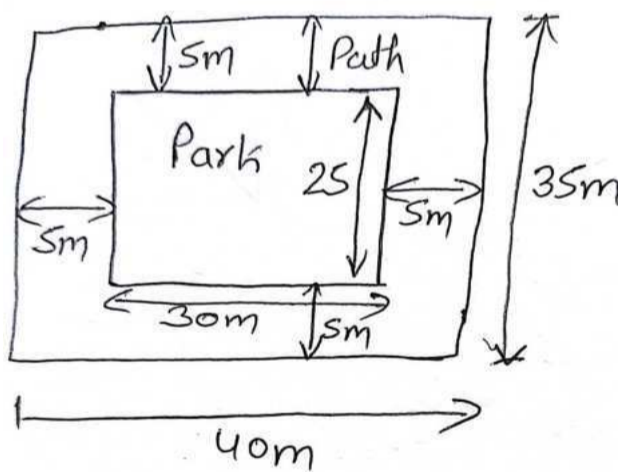
Breadth of the park = 25 m

A rectangle is a two-dimensional shape with four sides, four right angles, and opposite sides that are parallel and equal in length.

The formula for the area of a rectangle is $A = L * W$ where A is the area, L is the length, and W is the width of the rectangle.

The formula for the perimeter of a rectangle is

$P = 2 (L + W)$ where P is the perimeter, L is the length and W is the width.

Area of park = $30 \times 25 = 750 \text{ m}^2$ Area of the park and path = $40 \times 35 = 1400 \text{ m}^2$

Required area of the path = Area of the park and path – area of the park
 = $1400 - 750 = 650 \text{ m}^2$.

Cost of tiling per 10 m² = ₹ 1500Cost of tiling 1 m² = ₹ 150Cost of tiling 650 m² = $650 \times 150 = ₹ 97,500$.

∴ The cost of tiling the path is ₹ 97,500.

2. The perimeter of a square of side 25 cm is equal to the perimeter of a rectangle whose width is $\frac{2}{5}$ th the side of the square. Find the area of the rectangle.
- (A) 400 cm²
 (B) 500 cm²
 (C) 450 cm²
 (D) 600 cm²
 (E) Question not attempted

Ans (A)**Explanation:**

Side of square = 25 cm

Perimeter of square = $4 \times 25 = 100 \text{ cm}$ Width of the rectangle = $\frac{2}{5}$ of 25 cm = $\frac{2}{5} \times 25 = 10 \text{ cm}$

Let x be the length of the rectangle. Given that the perimeter of the square is equal to the perimeter of the rectangle.

∴ Perimeter of rectangle = $2 \times (x + 10) = 100 \text{ cm}$ ⇒ $x = \frac{100}{2} - 10 = 40 \text{ cm}$ Area of the rectangle = $40 \times 10 = 400 \text{ cm}^2$

3. Consider the isosceles trapezoid PQRS. The bases are $|BC| = 102 \text{ m}$, $|AD| = 62 \text{ m}$ and the arm $s = 29 \text{ m}$. Find the height of the trapezoid and the area of the trapezoid.
- (A) 21m and 1722 m²
 (B) 20m and 1722 m²
 (C) 22m and 1700 m²
 (D) 21m and 1700 m²
 (E) Question not attempted

Ans (A)**Explanation:**

A trapezium is a two-dimensional quadrilateral with one pair of sides that are parallel.

- The parallel sides of a trapezium are called 'bases'
- while the non-parallel sides are known as the 'legs' of the trapezium.
- The adjacent interior angles sum up to 180°.
- The sum of all the interior angles in a trapezium is always 360°.
- Area of trapezium = $\frac{1}{2} \times \text{Sum of parallel sides} \times \text{height}$.
- Perimeter of trapezium = Sum of all 4 sides

An isosceles trapezoid is a convex quadrilateral with two parallel sides and other two sides of equal length

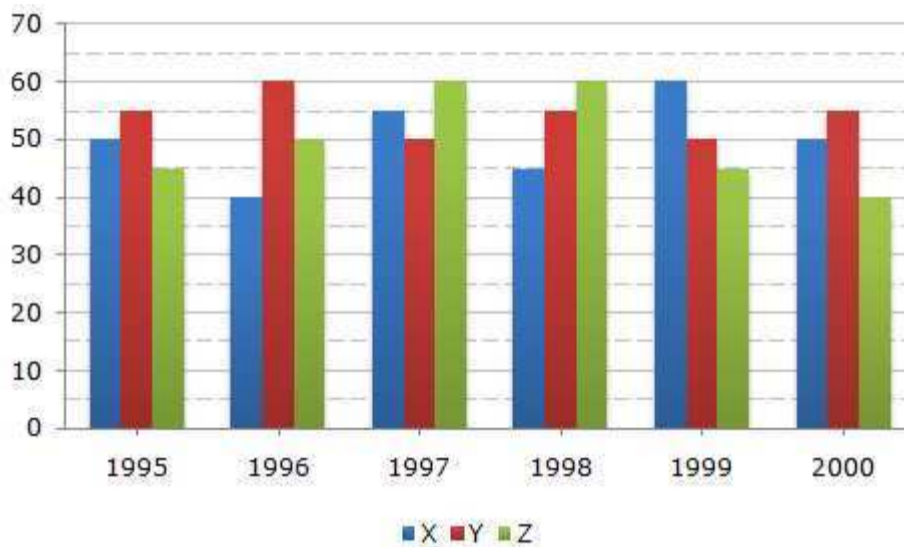
Let height = x = AE



Data Analysis (Tables, Bar diagram, Line graph, Pie-chart)

1. A soft drink company prepares drinks of three different flavours - X, Y and Z. The production of three flavours over a period of six years has been expressed in the bar graph provided below.

Production of Three Different Flavours X, Y and Z by a Company over the years (in lakh bottles)



For which flavour was the average annual production maximum in the given period?

- (A) X only
 (B) Y only
 (C) Z only
 (D) X and Y
 (E) Question not attempted

Ans (B)

Explanation:

Average annual productions over the given period for various flavours are:

For Flavour X = $\left[\frac{1}{6} \times (50 + 40 + 55 + 45 + 60 + 50) \right]$
 = 50 lakh bottles.

For Flavour Y = $\left[\frac{1}{6} \times (55 + 60 + 50 + 55 + 50 + 55) \right]$
 = 54.17 lakh bottles.

For Flavour Z = $\left[\frac{1}{6} \times (45 + 50 + 60 + 60 + 45 + 40) \right]$
 = 50 lakh bottles.

Therefore Maximum average production is for Flavour Y.

2. The following table gives the percentage distribution of population of five states, P, Q, R, S and T on the basis of poverty line and also on the basis of sex.

State	Percentage of Population below the Poverty Line	Proportion of Males and Females	
		Below Poverty Line	Above Poverty Line
		M : F	M : F
P	35	5 : 6	6 : 7
Q	25	3 : 5	4 : 5
R	24	1 : 2	2 : 3
S	19	3 : 2	4 : 3
T	15	5 : 3	3 : 2

If the population of males below poverty line for State Q is 2.4 million and that for State T is 6 million, then the total populations of States Q and T are in the ratio?

- (A) 1:3
 (B) 2:5
 (C) 3:7
 (D) 4:9
 (E) Question not attempted

Ans (B)

Explanation:

For State Q:

Male population below poverty line = 2.4 million.
 Let the female population below poverty line be x million.

Then $3:5 = 2.4 : x$

$3x = 2.4 \times 5 = 12$

$x = 4$

Total population below poverty line = $(2.4 + 4) = 6.4$ million.

If N_q be the total population of State Q, then,

25% of $N_q = 6.4$ million

$N_q = 6.4 \times 100 / 25 = 25.6$ million

For State T:

Male population below poverty line = 6 million.

Let the female population below poverty line be y million.

Then, $5:3 = 6 : y$

$y = 18/5 = 3.6$

Total population below poverty line = $(6 + 3.6) = 9.6$ million.

If N_t be the total population of State T, then,

15% of $N_t = 9.6$ million

$N_t = 9.6 \times 100/15 = 64$ million



Mean(Arithmetic, Geometric and Harmonic), Median and Mode

1. Find the median of the following data

Classes		0-1	1-2	2-3	3-4	4-5	5-6	6-7
		0	0	0	0	0	0	0
		1	2	3	4	5	6	7
		0	0	0	0	0	0	0
Frequency		5	1	1	3	2	1	5
			0	8	0	0	2	

- (A) 35.67
 (B) 35
 (C) 36.67
 (D) 36
 (E) Question not attempted

Ans (A)

Explanation:

For finding the median we create a table by adding the columns to given data. One column is for cumulative frequency which means sum of frequencies up to that class interval.

Then we find the median class for which class interval $(N/2)$ th frequency lies. Then median is given by

$$\text{median} = L + \left[\frac{(N/2 - f_0)}{f} \right] h$$

L is a lower interval of the median class

N is the sum of all frequencies

f_0 is the cumulative frequency of preceding median class

f is the frequency of the median class

h is the height of class interval

Class interval	Frequency (f_i)	Cumulative frequency
0-10	5	5
10-20	10	15
20-30	18	33 = f_0
30-40	30 = f	63
40-50	20	83
50-60	12	95
60-70	5	100

We know that

$$N = \sum f_i = 100.$$

Now, we need to find in which class $(N/2)$ th frequency lies.

We know that $N/2 = 50$.

So, frequency 50 lies in the class of 30.

So, the median class is 30-40.

We know that the formula of median is

$$\text{median} = L + \left[\frac{(N/2 - f_0)}{f} \right] h$$

By substituting these values in the formula we get

h is height of class interval ($h = 10$)

By substituting these values in the formula we

$$\Rightarrow \text{median} = 30 + \left(\frac{\frac{100}{2} - 33}{30} \right) \times 10$$

$$\Rightarrow \text{median} = 30 + \frac{17}{3}$$

$$\Rightarrow \text{median} = 35.67$$

Therefore, the median of given data is 35.67

2. Find the mean of the following data

Classes	0-10	10-20	20-30	30-40	40-50	50-60	60-70
	0	20	30	40	50	60	70
Frequency	5	10	18	30	20	12	5

- (A) 35
 (B) 36.6
 (C) 37.5
 (D) 35.6
 (E) Question not attempted

Ans (D)

Explanation:

For finding the mean we create a table by adding the columns to given data. One column is for midpoint of class, x_i and other column for product of frequency and midpoint of class $f_i x_i$

then we find mean using the formula

$$\text{Mean} = \frac{\sum f_i x_i}{\sum f_i}$$

Class interval	Frequency (f_i)	Midpoint of class (x_i)	$f_i x_i$
0-10	5	5	25
10-20	10	15	150
20-30	18	25	450
30-40	30	35	1050
40-50	20	45	900
50-60	12	55	660
60-70	5	65	325

By substituting the required values in the formula we get

**Probability**

1. A man and his wife appear in an interview for two vacancies in the same post. The probability of husband's selection is $(1/7)$ and the probability of wife's selection is $(1/5)$. What is the probability that Only one of them is selected ?

- (A) $2/7$
 (B) $1/7$
 (C) $3/4$
 (D) $4/5$
 (E) Question not attempted

Ans (A)**Explanation:**

Let A = Event that the husband is selected

An = Event that the husband is not selected

B = Event that the wife is selected

Bn = Event that the wife is not selected

Then, $P(A) = 1/7$ and $P(B) = 1/5$ $P(A_n) = 1 - 1/7 = 6/7$ and $P(B_n) = 1 - 1/5 = 4/5$ Required probability = $P[(A \text{ and not } B) \text{ or } (B \text{ and not } A)]$

$$= P[(A \text{ and } A_n) \text{ or } (B \text{ and } B_n)]$$

$$= P[(A \text{ and } A_n) + (B \text{ and } B_n)]$$

$$= P(A) \cdot P(A_n) + P(B) \cdot P(B_n)$$

$$= (1/7 \times 6/7) + (1/5 \times 4/5) = 10/35 = 2/7$$

2. One card is drawn from a deck of 52 cards, well-shuffled. Calculate the probability that the card will

- (i) be an ace,
 (ii) not be an ace.
 (A) $2/13$ and $11/13$
 (B) $1/13$ and $11/13$
 (C) $2/13$ and $12/13$
 (D) $1/13$ and $12/13$
 (E) Question not attempted

Ans (D)**Explanation:**

Well-shuffling ensures equally likely outcomes.

(i) There are 4 aces in a deck.

Let E be the event the card drawn is ace.

The number of favourable outcomes to the event E = 4

The number of possible outcomes $S = 52$ Therefore, $P(E) = n(E)/n(S) = 4/52 = 1/13$

(ii) Let F is the event of 'card is not an ace'

The number of favourable outcomes to $F = 52 - 4 = 48$ The number of possible outcomes $S = 52$ Therefore, $P(F) = n(F)/n(S) = 48/52 = 12/13$

3. A coin is tossed three times, find the probability of following events.

P: 'No head appears',

Q: 'Exactly one head appears' and

R: 'At Least two heads appear'.

(A) $1/2, 3/8, 5/8$ (B) $1/8, 1/8, 5/8$ (C) $1/8, 3/8, 1/2$ (D) $1/2, 1/8, 1/2$

(E) Question not attempted

Ans (C)**Explanation:**

The sample space of the experiment is:

Total possible outcomes 'S' = {HHH, HHT, HTH, THH, HTT, THT, TTH, TTT}

 $n(S) = 8$

Total possible outcomes in case of 'P' = {TTT},

Total possible outcomes in case of 'Q' = {HTT, THT, TTH},

Total possible outcomes in case of 'R' = {HHT, HTH, THH, HHH}

 $n(P) = 1, p(P) = n(P)/n(S) = 1/8$ $n(Q) = 3, p(Q) = n(Q)/n(S) = 3/8$ $n(R) = 4, p(R) = n(R)/n(S) = 4/8 = 1/2$

4. Find the probability of getting a numbered card when a card is drawn from the pack of 52 cards.

(A) $2/13$ (B) $9/13$ (C) $5/13$ (D) $7/13$

(E) Question not attempted

Ans (B)**Explanation:**

Total Cards = 52.

Let S be the sample space.

 $n(S) = 52$

Numbered Cards = (2, 3, 4, 5, 6, 7, 8, 9, 10) = 9

9 from each suit,

So total no of numbered cards = $4 \times 9 = 36$

Let E = Event of getting a numbered card

 $n(E) = 36$